

**Part I: 50points, Please describe your answers as complete as possible**

1. (12%) Describe what happens to unpolarized light incident on birefringent material when the OA is oriented as shown in each sketch in Fig. 1. Please comment on the following considerations: Single or double refracted rays? Any phase retardation? Any polarization of refracted rays? (OA stands for Optical Axis)

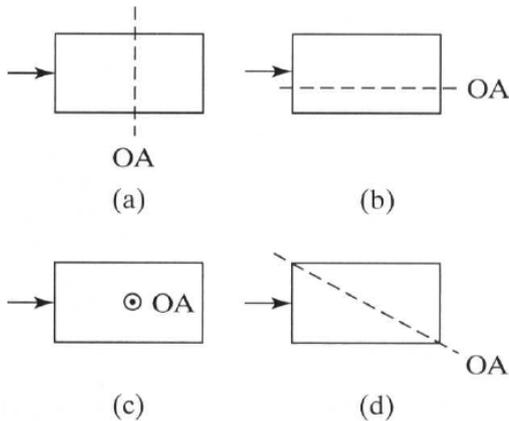


Fig. 1

2. (12%) A TEM<sub>00</sub> He-Ne laser ( $\lambda = 0.6328 \mu\text{m}$ ) has a cavity that is 0.34 m long, a fully reflecting mirror of radius  $R = 10$  m (concave inward), and an output mirror of radius  $R = 10$  m (also concave inward).

- Determine the location of the beam waist in the cavity.
- Determine the spot size at the beam waist,  $\omega_0$
- Determine the beam spot size  $\omega(z)$  at the left and right cavity mirrors.
- Determine the beam divergence angle for this laser.

3. (11%) Consider the transmission of 10 Gb/s signals at  $\lambda = 1500$  nm in a single-mode fiber, with a group velocity dispersion of  $D = 17$  ps/nm-km. Determine the pulse spreading after a transmission of distance 100 km.

4. (15%) A Fabry-Perot interferometer is to be used to resolve the mode structure of a He-Ne laser operating at 632.8 nm. The frequency separation between the modes is 150 MHz. The plates are separated by an air gap and have a reflectance ( $R$ ) of 0.999.

- What is the finesse of the instrument?
- What is the resolving power required?
- What plate spacing is required?
- What is the free spectral range of the instrument under these conditions?
- What is the minimum resolvable wavelength interval under these conditions?

**Part II: 50points**

1. (10%) A two-concave resonator has the cavity length of 10 cm, in which the radius of curvature is 20 cm for each mirror.
  - (a) What is the frequency difference between longitudinal modes? What is the frequency difference between transverse modes? Do the cavity configuration satisfy the transverse mode degenerate? (Please interpret your answer.)
  - (b) If the cavity length is tunable, what is the maximal cavity length for the stable condition?
2. (10%) What is the spectral hole-burning? Please use the gain curve to explain the multimode oscillation in an inhomogeneous broadening laser system.

3. (15%) The index ellipsoid for the KDP with a dc field,  $E_z$ , along the crystal z axis is given as

$$\frac{x^2}{n_o^2} + \frac{y^2}{n_o^2} + \frac{z^2}{n_e^2} + 2r_{63}E_zxy = 1,$$

where  $r_{63}$  is the electrooptic coefficient, and  $n_o$  and  $n_e$  are the indices for the ordinary and extraordinary rays, respectively. Calculate the  $V_\pi$ , the voltage yielding a retardation of  $\pi$ , for the wavelength of  $\lambda$ . Design an electrooptic amplitude modulator based on this KDP.

4. (15%) The optical fields transformed from  $E^{(\omega)}$  to  $E^{(2\omega)}$  in the second-harmonic generation satisfies the equation:

$$\frac{dE^{(2\omega)}}{dz} = -i\omega \sqrt{\frac{\mu}{\epsilon}} d[E^{(\omega)}(z)]e^{i(\Delta k)z},$$

where  $\Delta k = k^{(2\omega)} - 2k^{(\omega)}$ , and  $d$  is the nonlinear coefficient. Drive the conversion efficiency from  $\omega$  to  $2\omega$  for a crystal of length  $l$ . Explain the condition for the phase-matching and calculate the coherence length for the wavelength of  $1 \mu\text{m}$  and  $n^{(2\omega)} - n^{(\omega)} = 10^{-2}$ .

**Part III: 50points**

1. (a) Please draw the luminescence intensity of the LEDs as a function of the material energy bandgap. (5%)

(b) According to the (a) results, please proof its peak value at a frequency  $\nu_p$  determined by

$$h\nu_p = E_g + \frac{1}{2}kT. \text{ (5\%)}$$

2. GaAs has an intrinsic carrier concentration  $n_i=1.8 \times 10^6 \text{ cm}^{-3}$ , a recombination lifetime  $\tau=50 \text{ ns}$ , a bandgap energy  $E_g=1.42 \text{ eV}$ , an effective electron mass  $m_c=0.07m_0$ , and an effective hole mass  $m_v=0.50m_0$ . Assume that  $T=0 \text{ }^\circ\text{K}$ . Determine the (a) center frequency, (b) bandwidth, and (c) peak net gain within the bandwidth for a GaAs amplifier of length  $d=200 \text{ }\mu\text{m}$ , and thickness  $l=2 \text{ }\mu\text{m}$ , when 1 mA of current is passed through the device. (24%)

3. A conventional APD with gain  $G=20$  operates at a wavelength  $\lambda_0=1550 \text{ nm}$ . (a) If its responsivity at this wavelength is  $R=12 \text{ A/W}$ , calculate its quantum efficiency  $\eta$ . (b) What is the photocurrent at the output of the device if a photon flux  $\Phi=10^{10} \text{ photons/s}$ , at this same wavelength, is incident on it? (16%)